

BEYOND MIMESIS AND CONVENTION

Representation in Art and Science

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Truth and Representation in Science: Two Inspirations from Art

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Varieties of Truth in Art and Science

Not so long ago, pursuing the notion that the philosophies of art and science can inform one another in mutually productive ways might have been considered a cultured but fringe activity. Recently, however, philosophers more generally have awoken to the import of provocative and substantive analogies between practices of representation in art and science, and it is in the spirit of exploring such analogies that this essay is intended. My primary concern is to understand the nature of truth in the scientific context, and it will be my contention that this understanding requires an appreciation of a distinction between two different conventions of representation—one associated with practices of what I will call “abstraction”, and the other with practices of what is often called “idealization”. I believe that analogies to practices of representation in art can serve as valuable heuristics towards understanding how and in what manner scientific representations can be true.

The term “scientific representation” is commonly applied to many things, and would benefit from a more precise consideration than I can give it here. For present purposes, let me simply take such representations to include the usual items traditionally held to have representational status in the sciences, viz. theories and models, however these things are best defined, inhabiting the usual variety of ontological categories commonly associated with them: linguistic and mathematical entities; computer simulations; concrete objects; and so on. Other key concepts here will of course include those of abstraction and idealization, and I will have something to say about both and my reasons for focusing on these concepts in particular in due course. Let me begin, however, with the central concept whose explication this essay is intended to serve. Clearly, not all philosophers of science believe that the sciences are in the truth business, but an impressive diversity do, including different kinds of realists and empiricists. The former take the truths of science to include facts about

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unobservable entities and processes, and some of the latter acknowledge only truths about the observable, but all believe that scientific knowledge involves or at the very least aspires to substantive truths about the world, in some form or other. This is the first of two assumptions I will make here, at the outset.

The second assumption is that descriptions of entities and processes afforded by scientific representations are generally false, strictly speaking. I will not argue for this presently, but neither do I take it to be controversial. Even realists and empiricists who think that the sciences are in the truth business readily admit the hyperbole involved in suggesting that current representations (however circumscribed) are generally perfectly and comprehensively true. The history of the sciences has made a mockery of that suggestion in the past, and no doubt there is further mockery to come. It seems that anyone who endorses the idea of scientific truth as a reasonable aspiration requires some means of making sense of the idea that inaccurate representations can be close to the truth, and perhaps even get better with respect to truth over time. In the literature this requirement has motivated several accounts of "approximate truth", in terms of which, it is argued, one may understand such improvements. There would seem to be a widely held intuitive platitude concerning the notion of approximate truth, and Stathis Psillos (1999, 277) summarizes it nicely: "A description D ... is approximately true of [a state] S if there is another state S' such that S and S' are linked by specific conditions of approximation, and D ... is true of S' ." By itself, however, the helpfulness of this statement is impaired by the vagueness of the phrase "conditions of approximation". The remainder of this essay is essentially an attempt to clarify this phrase.

It will be my contention that the clarification required is wonderfully illuminated by drawing analogies to certain practices of representation in art, and as a final foreshadowing remark, let me mention briefly the path-breaking work in this area that informs several of the thoughts to follow. Nelson Goodman (1976) is celebrated for presenting a detailed analysis of the "symbol systems" in terms of which different forms of art express their content. At the end of his book on the subject, Goodman (1976, 262) says something particularly striking about the comparison between representations in art and in science:

... have I overlooked the sharpest contrast: that in science, unlike art, the ultimate test is truth? Do not the two domains differ most drastically in that truth means all for the one, nothing for the other? ... Despite rife doctrine, truth by itself matters very little in science.

It should be noted immediately that Goodman does not of course think that truth is unimportant in the sciences. Important truths about the natural world are indeed of great interest to scientists, and while one may admit that scientific laws are seldom true as they stand, we have an interest in "arriving at the nearest approximation to truth that is compatible with our other interests" (1976, 263). Ultimately, says Goodman, truth can be understood in terms of "a matter of fit" between theories and facts, and as it turns out, just this sort of "fitting" is characteristic of the relationship between art and the world (1976, 264). Truth in both domains should be understood in terms of approximating reality by means of representations. What more precisely

"fitting" and "approximating" mean in these contexts, however, is something I hope to explore here.

One reason Goodman suggests that truth *by itself* matters little, is that truth amounts to nothing unless one, in addition to having truthful representations, is properly acculturated with the conventions of representation in terms of which they express their content. It is precisely these conventions that I take to constitute the "conditions of approximation" whose explication is required in order to make sense of the notion of approximate truth, and so by exploring the former, I aim to shed light on the latter. In the following I will suggest that understanding two central features of scientific knowledge are crucial to illuminating these conditions of approximation, and it is here that analogies to representation in art may prove useful. The first of these features is a distinction between abstraction and idealization in connection with scientific representation, and the second concerns the pragmatics of scientific practice.

In the following section, "Preliminaries on Approximate Truth", I will briefly review extant approaches to the issue of approximate truth in the context of scientific knowledge. My goal here is modest: to convey in summary fashion the gist of these approaches and some reasons philosophers have worried about them. Leaving aside the details of proofs and potential resolutions of these worries, the main function of this discussion is to illuminate, by way of contrast, the approach taken here, which pays greater attention to the conventions of representation whereby scientific knowledge departs from truth at the outset, in its construction. The next section, "Truth in the Context of Abstraction and Idealization", considers the most central of these conventions recognized in contemporary philosophy of science—abstraction and idealization—and the ways in which one might articulate conceptions of approximate truth in either case. Idealization is the greater challenge here, and in the next section, "Denotation in Art, Reference in Science", Goodman's reflections on the nature of realistic and non-realistic artistic representation are exploited in furnishing a proposal for understanding the truth content of idealizations. In the fifth and final section, "Representations and Practice as Products and Production", a second analogy to representation in art, this time to the work and reception of some twentieth century avant-gardes, furnishes a poetic insight into the nature of scientific work, and its reception by philosophers in the latter twentieth century. In the process, I will make reference to pieces by Pablo Picasso, Jackson Pollock, and Yoko Ono.

Preliminaries on Approximate Truth

A moment ago I suggested that generally speaking, the knowledge contained in scientific representations is usually understood as approximately true at best. Three main families of accounts of approximate truth have emerged in the literature since the 1960s, and before considering the nature and relevance of abstraction and idealization in this context, it will serve us to have a synoptic overview of these approaches. I will refer to them respectively as the verisimilitude approach, due to Karl Popper, the possible worlds approach, formulated in different ways

by philosophers including Pavel Tichý, Ilkka Niiniluoto, and Graham Oddie, and the type hierarchy approach, offered by Jerrold Aronson, Rom Harré, and Eileen Cornell Way.

Popper was the first to give a definition of what he called "verisimilitude" or "truth-likeness". On his (1972, 231–236) view, scientific theories within a domain may exhibit increasing levels of verisimilitude over time, and this relative ordering can be expressed as follows. Consider a temporally-ordered sequence of theories concerning the same subject matter: T_1, T_2, T_3, \dots . Now for each of these theories, consider the set of all of its true consequences (for example, T_1^T) and the set of all of its false consequences (T_1^F). A comparative ranking of the verisimilitude of any two theories can be given, suggests Popper, by comparing their true and false consequences. For any theory T_n , and any previous theory $T_{<n}$, T_n has a higher degree of verisimilitude than $T_{<n}$ if and only if either of the following statements is true (" \subseteq " here stands for set-theoretic inclusion, and "<" for proper inclusion):

1. $T_{<n}^T \subset T_n^T$ and $T_n^F \subseteq T_{<n}^F$
2. $T_{<n}^T \subseteq T_n^T$ and $T_n^F \subset T_{<n}^F$

Though intuitive, this account is unfortunately afflicted by fatal difficulties, first described by David Miller (1974) and Tichý (1974). As these and other authors have proven formally, one can show that in neither the case of 1 or 2 above can both conjuncts be satisfied together. It turns out that, on Popper's definition, in order that T_n have greater approximate truth than $T_{<n}$, T_n would have to be true *simpliciter*. Thus, on this view, one false theory cannot have more approximate truth than another, and this rather defeats the aim of providing an understanding of what it could mean to rank false theories with respect to truth.

The precise formulation of the possible worlds approach (also called the "similarity" approach) varies between different authors, but what follows is a general characterization of it. The basic idea is first to identify the truth conditions of a theory with the set of possible worlds in which it is true, and then to calculate what one may call "truth-likeness" by means of a function that measures the average "distance" between the actual world and the worlds in that set. In this way, one may generate an ordering of theories with respect to truth-likeness. For example, consider the class of atomic propositions entailed by a theory, each attributing a specific state to a particular; possible worlds here are described by distributions of truth values across these atomic propositions. The greater the agreement between a given theory and a theory correctly describing the actual world, the greater the former's truth-likeness.¹

Though less clearly undermined by objections than Popper's account, the possible worlds approach is itself subject to two important controversies. First, Miller (1976) argues that on this view, measures and relative orderings of truth-likeness

¹See Tichý (1974, 1976, 1978), Niiniluoto (1984, 1987, 1999), and Oddie (1986a, b, 1990). Niiniluoto (1998) summarizes the different formulations associated with this approach.

are language-dependent: logically equivalent theories may have different degrees of truth-likeness depending on the language in which they are expressed, and the relative truth-likeness of two theories may be reversed when translated into another language with logically equivalent predicates. Second, Aronson (1990) shows that on this view, the truth-likeness of a proposition (whether true or false) depends on the number of atomic states under consideration, and it is at least questionable whether the truth-likeness of propositions concerning states of affairs *other* than that described by the proposition at issue should be relevant in this way. Disputes concerning these charges continue to surround this approach today.

Finally, a third approach to approximate truth analyzes truth-likeness in terms of similarity relationships between nodes in type hierarchies: tree-structured graphs of types and subtypes.² The nodes represent concepts or things in the world, and links between them represent relations between concepts or things. As an illustration, consider the standard biological taxonomy of organisms divided into kingdoms, phyla, and so on down to species. Similarity here is defined with respect to locations within type hierarchies. In order to show that dolphins are more similar to whales than tuna, for example, one calculates their degrees of similarity to one another by means of a weighted difference measure, comparing the properties these types share and those in which they differ. Now consider an analogous comparison between a node in a theoretical type hierarchy and a corresponding node in the actual type hierarchy of the world. Truth-likeness is measured by the "distance" between a theoretical claim about a type and the correct description of that type, reflecting the degree of similarity of the nodes with which these descriptions are associated. The most striking difficulty with this approach is that it appears to require the existence of a unique type hierarchy of the world. Lacking this, it seems there is no determinate answer to the question of what a node in a theoretical type hierarchy should be compared to. As Psillos (1999, 277) observes, on this view, significantly different type hierarchies would lead to different measures of approximate truth, and the assumption that nature admits of only one correct taxonomy is controversial at best.

Each of the three approaches to approximate truth just outlined face interesting challenges, and it is not my intention here to see whether these challenges can be met. My goal in reviewing them has been rather to set the stage for what I take to be a more general complaint, to be leveled against all three. None of these established approaches to approximate truth pays much if any explicit attention to the qualitative dimensions of the concept, which concern the ways in which theories and models typically diverge from truth in the first place. It is precisely a better understanding of these details, I contend, that is crucial to understanding the nature and truth content of scientific representations, and it is in this context that I will take inspiration from certain analogies to practices of representation in art. Understanding *how* scientific representations give inaccurate accounts of their subject matter is an important precursor to thinking about approximate truth, for as we shall see, there are different *kinds* of representational inaccuracy, and as a consequence, I will suggest, the

²See Aronson (1990), and Aronson et al. (1994, 15–49).

concept of approximate truth is best explicated differently in different circumstances, depending on the relevant modes of inaccuracy. Extant approaches to the concept place no emphasis on these differences, which I take to be central. In the following section, I will attempt to explain what these differences are, and why they are so important.

Truth in the Context of Abstraction and Idealization

Let us turn now to consider the ways in which scientific theories and models are constructed so as to deviate from the truth. There are, I believe, two such ways, and I will call them *abstraction* and *idealization* respectively. In focusing on these two practices specifically, I am drawing on a recently established tradition in the philosophy of science that regards them as the primary means by which scientific representations are constructed and related to the worldly phenomena they target. I will not explore the nuances of this rapidly growing literature here; let it suffice to say that while there are, of course, idiosyncratic differences in various presentations of the relevant concepts, the fundamental ideas are widely shared.³ In the following, I will sketch my own view of them, which is faithful to the central tenets of this recent tradition in thinking about scientific representation.

Roughly put, an abstract representation is the result of a process of abstraction; that is, one in which only some of the potentially many factors that are relevant to the behavior of a target system are built into the representation. In such a process other parameters are ignored, either intentionally or unwittingly, so as to permit the construction of a tractable representation. A commonly discussed example of this is the model of the simple pendulum. Here, among other simplifying assumptions made in the construction of the model, one simply omits the factor of frictional resistance due to air. The reason such omissions are thought to compromise the truth of resultant representations is not merely the fact that they leave out theoretically important aspects of the systems they represent, but that even more importantly, in doing so, they also generate predictions regarding these systems that deviate from reality. By omitting factors that play a causal role in determining the values of certain parameters, for example, abstractions often fail to be accurate in their estimations of them. The greater the discrepancy between the output of an abstract representation and the behavior of its target system, the less approximately true it may seem.

On the other hand, an idealized representation is the result of a process of idealization; that is, one in which at least one of the parameters of the target system is represented in a way that constitutes a distortion or a simplification of its true nature. In such a process, one is not excluding parameters, as in abstraction, but incorporating them, again either intentionally or unwittingly, in such a manner as to represent them in ways they are not—indeed, as I shall use the term, in ways they could not

³For some of the most influential and comprehensive discussions, see McMullin (1985), Cartwright (1989, Chapter 5), Suppe (1989, 82–83, 94–99), and Jones (2005).

possibly be. Idealized representations thus furnish strictly false descriptions of their counterparts in the world. For example, in the *Principia*, Newton assumes that the sun is at rest in his derivation of Kepler's laws of planetary motion. According to his own theory, however, this would require that the sun have infinite mass, and Newton clearly did not believe this to be the case. On his understanding, the sun experiences small amounts of motion as a consequence of the attractions of other bodies, and so, the "attribution" of infinite mass constitutes an idealization. Abstraction and idealization are not mutually exclusive processes, and consequently, representations are often both abstract and idealized. A model of a frictionless plane, for instance, is an abstraction because it leaves out frictional forces associated with the plane, and if no surfaces are totally frictionless, the model also incorporates an idealization. Elements of idealization enter the picture when representations describe systems in ways they could not be, given the laws of nature that obtain in our world.

Now, given these two practices of deviation from the truth, how should one think about the approximate truth of scientific representations? It seems to me that there is a straightforward answer to this question in cases of pure abstraction—that is, in cases of abstraction which incorporate no idealization—and a less obvious answer in cases of idealization. Regarding the former, there would seem to be no impediment to thinking of a pure abstraction as true *simpliciter*, if only in connection with a certain class of target systems. Pure abstractions correctly describe certain features of things in the world, even if they do not describe all of the properties and relations potentially relevant to the phenomena at issue. It is natural, of course, to view abstractions as yielding false descriptions because of their omissions and resultant inaccuracies of prediction. But in the case of pure abstractions, where no idealization is involved, target systems in which only those parameters represented contribute to the behavior of the system are presumably possible; if they were not, this would indicate the presence of an idealization. Therefore, pure abstractions are perfectly accurate representations of *some* nomically possible target systems (that is, ones that could exist, given the laws of nature that obtain in our world), even if they are impoverished representations of other, more complex ones. Clearly, one may apply a pure abstraction to a more complex system it does not correctly describe, but this should not be taken to discredit the truth of the representation in connection with systems it *does* correctly describe. Neglecting air resistance usually counts as an error of omission, but it would not be in connection with a system in a vacuum.

This suggests a straightforward articulation of the notion of approximate truth *qua* abstraction. Consider all of the parameters potentially relevant to the behavior of a particular target system. Degrees of approximate truth are correlated here with the extent to which representations incorporate these parameters. The greater the number of factors built into the representation, the greater its approximate truth. This suggestion for assessing relative degrees of approximate truth does justice, I think, to the intuition that higher degrees of abstraction may correspond to lesser degrees of truth, but without failing to appreciate that abstractions may yet characterize some things perfectly accurately. Pure abstractions yield correct descriptions of certain classes of target systems while being more or less approximately true in

application to others, and here we have our first insight into what "conditions of approximation" means in the analysis of approximate truth. In these cases, conditions of approximation can be understood simply in terms of how much information a representation yields, or its comprehensiveness, relative to a specific kind of target system, or class of systems.

In cases of idealization, however, one requires a rather different understanding of the relevant conditions of approximation. For here, unlike in cases of pure abstraction, one does not have the luxury of representations that accurately characterize at least some nomically possible phenomena. Idealizations are more egregiously fictional than abstractions; they constitute not mere omissions, but distortions of things in the world. Models in classical mechanics, for example, generally treat the masses of bodies as though they are concentrated at extensionless points, but given the nature of mass as we understand it, in accordance with the laws of nature, it cannot be concentrated this way in any world such as ours, where particulars with masses exist. What information about the world is contained in fictions such as these?

A failure to grapple seriously with the qualitative nature of idealization is, I believe, a defect of extant accounts of approximate truth. Consider my illustration earlier of the possible worlds approach, in which one considers the class of atomic propositions entailed by a theory, each attributing a specific state to a particular, as a means towards evaluating its approximate truth. In cases of pure abstraction, one may justifiably claim here that the greater the extent to which a representation yields true descriptions of systems in the world, the greater its truth-likeness. Idealizations, however, do not generally give true descriptions of atomic states of affairs, for they are constructed in such a way as to characterize their objects in a distorted manner. Likewise, consider again the type hierarchy approach, where one calculates degrees of similarity between theoretical propositions and true ones by performing weighted difference measures involving the properties these propositions describe in common and those in which they differ. Arguably, however, idealized characterizations may describe few *if any* properties in common with true theories, because they correctly describe fictional properties, not actual ones. The conditions of approximation relevant to assessing approximate truth *qua* idealization must be understood differently, I think, than the relevant conditions of approximation *qua* abstraction.

Denotation in Art, Reference in Science

In order to appreciate how idealizations bear on the notion of approximate truth, let me now return to Goodman, and draw a first analogy to representation in art. In the first section, "Varieties of Truth in Art and Science", I quoted Goodman as suggesting that in both art and the sciences, successful representation is a matter of fitting or approximating things in the world. Let us now consider this suggestion in more detail, beginning with an examination of Goodman's reflections on the nature of realistic and non-realistic representation. It is precisely this distinction, I will

argue, that is important to understanding the "truth content" of idealized theories and models. The contrast between the nature of this content in cases of abstraction and idealization will provide crucial insight into how different contexts of representation call for a flexible approach on the part of those seeking to explicate the concept of approximate truth.

In the opening sections of his major work on artistic representation, Goodman (1976, 34) considers the question of how best to understand the nature of realism in this context. His answer appears at first both provocative and negative: "Surely not [in terms of] any sort of resemblance to reality". Goodman does not provide much help with the ambiguous term "resemblance", here, but on any obvious reading, his answer presents a *prima facie* puzzle of interpretation. If one interprets "resemblance" narrowly to mean "similarity in appearance", this might seem a strange claim regarding much art, though not perhaps regarding science; in the latter case one hardly expects mathematical equations (for example) to share similarities in appearance with acids and bases or populations of organisms. Reading "resemblance" more broadly, as "having some feature or features in common", the puzzle of interpretation extends even to the scientific case, since most philosophers of science hold that at least some parts of our best theories and models do, in fact, have features in common with their target systems, such as commonalities in structure (whether concerning observable or unobservable parts of the world). These interpretive puzzles, however, are resolved with the clarification that for Goodman, realism is by no means inconsistent with resemblance in either of the senses just mentioned. His point is rather to emphasize that, as suggested earlier, realism of representation is only achieved in special circumstances, *viz.* those in which agents considering the representation have been acculturated with the system or systems of representation that have been employed in constructing it.

Consider a realistic picture, painted in ordinary perspective and normal colour, and a second picture just like the first except that the perspective is reversed and each colour is replaced by its complementary. The second picture, appropriately interpreted, yields exactly the same information as the first. And any number of other drastic but information preserving transformations are possible. Obviously, realistic and unrealistic pictures may be equally informative; informational yield is no test of realism. ... The two pictures just described are equally correct, equally faithful to what they represent, provide the same and hence equally true information; yet they are not equally realistic or literal. ... Just here, I think, lies the touchstone of realism: not in quantity of information but in how easily it issues. And this depends upon how stereotyped the mode of representation is, upon how commonplace the labels and their uses have become (Goodman 1976, 35–36).

Goodman is a conventionalist about systems of representation: anything can represent anything else, subject to appropriately internalized conventions. As a consequence, one and the same representation can be realistic or not, depending on whether the relevant conventions have been internalized by the viewer or user.

Several fascinating issues concerning conventionalism and representation are raised by this and surrounding passages, but for present purposes, let me simply extract one key point: an understanding of the relevant and potentially different conventions of reading information from representations is crucial to how one

understands that information. This point bears directly on my contention that if one is to have a genuinely informative account of what it means to say that scientific representations are approximately true, one must understand the different conditions of approximation exemplified by abstraction and idealization. These different conditions, I suggest, should be understood in terms of different conventions of representation.

Having already considered the way in which pure abstractions approximate reality, let us do the same now for idealizations. One last point arising from Goodman's discussion of artistic representation will prove useful in this regard. Goodman (1976, 5) suggests that "the core of representation" is denotation. That is, in order for x to represent y , x must be a symbol for, or stand for, or refer to y . Symbols here include "letters, words, texts, pictures, diagrams, maps, models, and more" (1976, xi). In Goodman's terms, denotation is simply a particular species of reference, pointing from representations to things represented. And with this in mind, here finally is the first feature of artistic representation that I believe furnishes a provocative analogy for those hoping to understand the nature of approximate truth in science: just as in the case of art, where successful representation can be a function of denotation, in the sciences, successful representation can be a function of reference, even when theories and models offer idealized descriptions of the properties and relations of their target systems. In the first instance, idealizations "fit" or "approximate" reality by latching on and successfully referring to aspects of it. Let us consider this suggestion in some detail.

To be sure, emphasizing reference is hardly novel in the philosophy of science, especially in discussions of scientific realism. Entity realists are especially well known for this, holding that under conditions in which one has significant evidence of an ability to manipulate or otherwise systematically exploit the causal properties of entities, one has good reason to believe that such entities exist, even while withholding belief from the theories that describe them. It is for this reason that entity realism can be cast as a response to challenges to realism posed by the history of science, which provides ample evidence of theoretical descriptions changing over time. Hacking (1983, Chapter 6), for example, contends that one may continue to refer to the same causal entity despite changes in the theories that describe it, and this furnishes a stable point around which realists can organize their knowledge claims regarding unobservables. Despite the fact that theories are false and likely to change, says the entity realist, there are conditions under which one has good reason to think that unobservable terms refer, and will continue to refer. Interestingly, the importance of relations of reference has never really shaped thinking about approximate truth, but it is my contention here that they are clearly relevant to understanding the differential truth content of pure abstractions and idealizations. Insofar as *true* (that is, non-idealized) claims about entities and processes can be extracted from idealizations, these are for the most part claims of successful reference, not the more detailed descriptions of target systems that one may associate with cases of pure abstraction.

This should not be taken to suggest, of course, that merely appealing to reference can save realist blushes. This appeal on behalf of entity realism is controversial,

even amongst scientific realists. Many question whether it is coherent to be a realist merely about certain entities described by theories, since causal manipulations and exploitations seem to be based on further and substantial parts of those theories. And as I have argued elsewhere (2007, Chapter 2), there does seem to be something anachronistic in the suggestion that scientists from different periods in the history of scientific investigation into an entity all believe in the same thing. In order to be more compelling, the realist's story must be told at a deeper level, with respect to specific properties and relations on which existential claims are based, and that are likely to survive (if only as limiting cases) in theories over time. Despite what I take to be serious difficulties, however, there is an important insight at the heart of entity realism: degrees of belief in unobservable entities are generally and rightly correlated with the extent of one's causal contact with those entities. There are no stronger grounds for belief in an entity than an impressive ability to systematically exploit its causal properties, and less impressive abilities rightly ground more attenuated beliefs. On the impressive side of this continuum, claims of reference are concomitantly strong. For those of a strict empiricist bent, the same point can be made, *mutatis mutandis*, regarding observable entities.

Having emphasized the notion of reference, and having gestured towards some of the nuances that must be taken into consideration concerning reference in this context, I am now in a position to describe what it means for one theory to be more or less approximately true than another *qua* idealization, and to contrast this with cases of pure abstraction. When it comes to truth, even the best idealizations contribute primarily existential claims. This does not mean, however, that all idealizations are on a par when it comes to the approximate truth of the more substantive descriptions they provide. Some idealizations approximate true descriptions of properties and relations better than others, and this is an important consideration in assessing their relative approximate truth. The relevant notion of approximation here is usually specified mathematically. One can define mathematically how Newtonian descriptions of certain properties approximate those of special relativity, for example, by showing how the equations of Newtonian mechanics are limiting cases of relativistic equations. The ideal gas law assumes that molecules of gas are point particles and that there are no forces of attraction between them, but it is possible to take into account both the space occupied by molecules of gas and small forces of mutual attraction. Thus, while the van der Waals equation generates values for various properties that approach those given by the ideal gas law at lower pressures (larger volumes), it yields different, more accurate values at higher pressures (smaller volumes).⁴ The Van der Waals equation, over certain ranges of pressure, volume, and temperature, describes the natures of these properties and their relations more accurately than the ideal gas law.

Earlier I credited Psillos with a precise statement of what I take to be a widely-held intuitive platitude regarding approximate truth, to the effect that a description

⁴McMullin (1985, 259) contains a nice discussion of this and similar cases.

is approximately true of a state if it can be “linked by specific conditions of approximation” to a true description. It was precisely because of a lack of clarity regarding the question of what these “conditions of approximation” might be that I undertook to focus attention on them, with the goal of generating a more satisfying explication of the concept of approximate truth. I believe the various pieces of the puzzle are now in hand. When representations deviate from true characterizations of their target systems, they do so via abstraction, or idealization, or in many cases both. I have argued that insofar as representations are abstract, approximate truth may be gauged in terms of the numbers of potentially relevant features of their target systems they incorporate, so that theories incorporating greater numbers of these features may be thought of as more approximately true than those incorporating fewer. Pure abstractions yield descriptions of properties and relations that are true *simpliciter* of certain classes of target systems, and that may be more or less approximately true in application to others. The notion of approximate truth *qua* abstraction is thus simply the notion of comprehensiveness, generally assessed in connection with a specific target system, and the relevant condition of approximation here is the extent to which the numbers of factors incorporated into a representation match up with those in the target systems to which it is applied.

The notion of approximate truth *qua* idealization is importantly different, for here the issue is not the comprehensiveness of representations, but in the first instance, their successful reference, and thereafter, the accuracy with which they characterize the natures of the specific parameters they represent. Unlike pure abstractions, idealizations do not generally offer true characterizations of the properties and relations they concern, even if they do permit ontological claims, in virtue of successful reference. By reducing the number of idealized assumptions or the extent to which they idealize—by de-idealizing—one describes target systems in ways that admit of greater degrees of approximate truth. Unlike the case of abstraction, however, where improving a representation is simply a matter of increasing the number of potentially relevant factors it incorporates, there is no reason to expect that processes of de-idealization should follow any common pattern from one domain of theorizing to the next. There are many ways of incorporating idealized assumptions into representations, and the ways in which one describes possible de-idealizations may vary in just the way that idealizations do. In any case, whatever these variations, idealized representations may be improved in ways determinable in specific instances. Approximate truth *qua* idealization concerns the degree to which a representation that has successfully latched on to an aspect or aspects of some target system resembles a non-idealized representation of that system, where degrees of resemblance are defined in specific cases. The relevant condition of approximation here is not comprehensiveness, but successful reference, and degrees of distortion or simplification of the specific properties and relations targeted.⁵

⁵Interesting questions naturally arise here concerning whether, in the context of scientific (if not artistic) representations, distortions can be so severe as to sever relations of reference, whether in such cases it is reasonable to speak of idealizations of target systems at all, and so on. For some thoughts on these issues, see my (2009).

Let me sum up the import of the first analogy furnished by representation in art before turning to a second. When viewing a painting or a sculpture, one may extract more or less information regarding the things it represents, depending on the amount of information it contains, and the extent to which one has mastered the conventions of representation it employs. At one end of this spectrum is what Goodman calls realistic representation in art. Here, the viewer is sufficiently acculturated with some relevant system or systems of representation to derive significant information about the subject matter represented. At the other end of the spectrum representations may convey very little information, but information nonetheless. Consider the representational content of paintings, for example. Just one of the reasons Pablo Picasso's *Guernica* (1937) is one of the most celebrated artworks of the twentieth century is its captivating representational power. Its subject is the bombing of the Basque town of Guernica by Hitler's and Mussolini's air forces, with the complicity of Franco, during the Spanish Civil War. Aspects of the work, such as the figures of a bull, a dead baby in the arms of a screaming woman, a speared horse, the broken body of a soldier, and so on, represent various things with greater and lesser degrees of realism. The painting taken as a whole also has representational content. Among other things, for instance, it represents the rising threat of European fascism.⁶ Insofar as the painting represents this, however, it is not depictive, but merely denotative. It does not provide much in the way of “description” beyond the existential “claim” it makes concerning the presence of a terrifying danger.

Scientific representations also yield information about their subject matter, but whether they do so by providing true characterizations of specifically chosen parameters, or by distorting the parameters to which they successfully refer, will depend on how abstract and idealized they are. The contrast between depiction and mere denotation as a central feature of representation in art is an analogy for the contrast between truth and mere reference as a central feature of representation in the sciences. Higher degrees of approximate truth can be understood in terms of improved representations of the natures of target systems in the world, and this improvement can be mapped along two dimensions: how many of the relevant properties and relations one describes (abstraction), and how accurately one describes them (idealization). This simple formula, combined with an understanding of the conditions of approximation involved in the practices it describes, comprises an explication of the principal notions at stake in making sense of the idea of approximate truth.

Representations and Practice as Products and Production

Let me now turn, finally, to the second analogy between representation in art and science I promised at the start. This one also concerns approaches to truth, but in a rather different way than the first. For quite apart from the question of whether one can make sense of the notion of approximate truth, it should be noted that in the

⁶See Suarez (2003, 236), for a discussion of this painting and associated literature.

philosophy of science, there is no consensus regarding what *sorts* of scientific claims one ought reasonably to regard as true or approximately true in the first place. While realists defend the reasonableness of believing scientific claims concerning both observable and unobservable aspects of target systems, various critics, including varieties of empiricists and instrumentalists, accept only the former. My goal in this final section is to employ a second analogy of representation between art and science so as to extend a bridge between these opposing camps. In part because of their obsession with unobservable things, realists are often guilty, I believe, of failing to note the significance of the observable. Certainly, realists like everyone else regard observable consequences as furnishing tests of the accuracy of representations, but I have something else in mind here. In scientific practice, one is often primarily concerned with whether and to what extent theories, models, procedures, tests, etc. *work*. Can we use them to make faster computer chips, manage eco-systems, and successfully complete the astounding variety of tasks associated with laboratories and fieldwork across the globe every day? Success in practice is measured in terms of observable consequences, and there is a strong current of pragmatism built into everyday scientific pursuits. The pragmatist's test of epistemic significance is utility, and utility is assessed by means of observables.

Antirealists often intimate that realist interpretations of scientific knowledge are out of touch with the everyday worlds of real science, as opposed to the rarefied philosophical worlds of imagined science. The prevalence of empirically adequate idealizations and pure abstractions applied to systems they do not correctly describe serves to fuel this skepticism. It is for this reason that the idea of approximate truth, and more specifically, the idea that different sorts of truths may be contained within different sorts of scientific representations, is so important to realism. Armed with an understanding of the truth content of both idealizations and pure abstractions applied to systems they do not correctly describe, one may connect desiderata that skeptics generally believe to be independent of one another: the generation of observable predictions within acceptable margins of error (the goal of much scientific endeavor); and the uncovering of facts regarding unobservables that underlie these predictions. In the first section of this essay, I suggested that a consideration of two important features of scientific knowledge would facilitate an account of the concept of approximate truth. The first of these was the distinction between abstraction and idealization. The second concerns the pragmatic dimensions of scientific practice, and this topic, I believe, is intimately connected to the first. Let me move on to the second, now, by means of a second analogy to representation in art.

The history of twentieth-century art is, to a great extent, the history of the avant-gardes and their forms of "abstraction". Realistic conventions of representation, in Goodman's sense, were supplemented by varieties of experiments seeking to realize different sorts of conventions, both in the service of representation and even, in some cases, in the service of *non*-representational expression. These experiments initiated traditions that we now recognize as familiar artistic movements such as Cubism, Surrealism, Constructivism, and Abstract Expressionism. The disparate approaches of the avant-gardes exemplified a shared rebellion against traditional approaches to representation, and a striking feature of much of this work is an increasing focus

on processes of art production, as opposed to the precise visual properties of the products of these processes. This is not to say, of course, that in many or most of these cases, products such as paintings and sculptures ceased to be important to artists and their critics. Rather it is to note that many of these artistic pioneers were self-consciously and sometimes primarily interested in reflecting on the nature of artistic representation itself, paying great attention, for example, to the nature of the canvas as a two-dimensional surface, as opposed to the task of realistically representing three-dimensional subjects. This is one, partial interpretation of the motivations of analytic Cubism, but it is also a recurring theme in other movements.

Consider the emergence of Abstract Expressionism in the 1940s and 1950s. One of the defining features of this work is a commitment to *expressing* emotional and other cognitive states of the artist, as opposed to depicting them as such. The methodology of Jackson Pollock is legendary in this regard: Pollock would drip, fling, and otherwise propel paint onto canvases placed on the ground, by means of controlled and sometimes highly athletic movements. The process of creation here is a central part of the content of the work. The artists of this and other movements increasingly emphasized the materiality of the process of painting, as opposed anything like realistic representation. The surface of the canvas, its shape, the thickness of the paint, and so on, took on a new significance. Co-opting the slogan of the American art critic Clement Greenberg (2003/1939, 539), this is "art for art's sake".

The rise of performance art may exemplify this tendency towards attaching greater significance to processes involved in the creation of art as opposed to its products per se better than anything else. Works associated with the Fluxus movement, for example, such as Yoko Ono's *Cut Piece*, may serve to illustrate the point. *Cut Piece* was performed by Ono four times, in Kyoto (1964), Tokyo (1964), New York (1965), and London (1966). During these events, the artist sat on a stage while members of the audience approached, individually and in succession, to cut pieces of clothing from her body with a pair of scissors. The piece is variously interpreted as engaging with issues of female vulnerability, sexual violence, and gender politics; and as a response to the horrors of war and the threat of nuclear annihilation.⁷ Here as in all work in the performance art genre, the idea of a process takes on so much significance that *it* now is the central focus of the artwork. What matters is an event or a series of events. The idea that the value of the performance resides in any further output is completely lost. Of course, photographs of works of performance art are very important for purposes of discussion and art criticism, but such outputs are considered mere documents of the art form, not things that are important in their own right, and certainly not things that are the proper focus of attention when considering the nature or significance of the work.

Keeping in mind this analogy of a transition in focus from products to production, let us now return to the case of the sciences, and give due consideration to the pragmatic dimension of scientific practice. Focusing on processes of production

⁷For an insightful discussion of the variety of interpretation and the literature surrounding it, see Bryan-Wilson (2003).

led artists to a dizzying array of less-than-realistic representations. Analogously, focusing on processes of detection, experiment, and the innumerable tasks constituting everyday scientific work leads scientists to create ingenious abstractions and idealizations. In the successful pursuit of much of this work, one does not require anything like truth *simpliciter*. One of the main reasons abstractions and idealizations are so ubiquitous in the sciences is that they facilitate these tasks so well, within the degrees of accuracy and precision required in the contexts of particular scientific endeavors. Indeed, it is often the case that less approximately true representations are preferred to more approximately true ones. For while both may generate predictions that are adequate to specific endeavors, simpler though less approximately true theories and models are, generally, more easily taught, learned, and used.

Furthermore, the epistemic virtues of inaccurate representations often extend beyond their mere contextual adequacy. Scientists routinely apply pure abstractions and idealizations to phenomena whose properties and relations they do not correctly describe, but that is not to say that in such cases, representations yield no truths.⁸ The classical theory of gases idealizes several properties of gas molecules and their relations to one another, but nevertheless has the (putatively) true consequences that there are molecules composing gases, and that they have properties such as mass. These are truths about particulars and properties that follow immediately from successful reference, but other truths stemming from idealization arguably go further. Frictionless surfaces are ideal, but models of spherical objects sliding down frictionless inclined planes correctly describe the motions of these objects as linear. Newtonian models of the earth-moon system are idealized, but correctly represent the mass of the earth as being greater than that of the moon. Idealizations generate substantially less truth *simpliciter* than pure abstractions, but what truths they do yield may nevertheless add to their pragmatic utility.

The emphasis on production as opposed to products in art and science has an echo in the intellectual traditions that study these practices. A delightful symmetry can be found, for example, in the juxtaposition of twentieth-century art criticism and post-positivist philosophy of science. One of the recurring themes of critiques of logical positivism was that it was too absorbed with normative projects based on rational reconstructions of the products of the sciences, such as theories and models, and as a consequence, it is argued, the positivists found themselves out of touch with actual scientific practice. Thus it comes as no surprise that the demise of positivism in the twentieth century was accompanied by the rise of the history of science as an essential tool for philosophers. Much post-positivist philosophy of science takes the details of scientific practice as its focus, thereby de-emphasizing considerations of the epistemic status of its products. And thus, the word "truth" does not appear in Kuhn's iconic essay in the history and philosophy of science, *The*

⁸I owe thanks to Martin Thomson-Jones and Juha Saatsi for illustrating this point with some of the following examples.

Structure of Scientific Revolutions, and Hacking (1983) is ultimately more interested in intervening in the natural world than representing it.

This sort of pragmatism is something that realists must take to heart in grappling with the concept of approximate truth. It is a concept that is differently instantiated by means of different representational relationships, involving true descriptions of properties and relations in some cases, and little more than successful reference in others. Some representations are purely abstract, in which case they yield a multitude of true descriptions of certain classes of phenomena. Other representations are heavily idealized, and consequently their truth rests primarily in existential claims, and in the extent to which their descriptions of properties and relations measure up to true descriptions, in ways specifiable in connection with specific target systems. Most cases of scientific representation are neither pure abstractions nor pure idealizations, of course, but rather mixtures of both, in different proportions and to varying degrees. The concept of approximate truth is thus heterogeneous, to be explicated as may be appropriate in particular cases, within the myriad contexts of representation to which it may be applied.

It is thus the conclusion of this paper that in the sciences, approximate truth is best understood as a virtue that is multiply realized by means of different kinds of representational relationships between scientific products such as theories and models on the one hand, and target systems in the world on the other.⁹ These different conventions of representation reflect the degrees to which theories and models abstract and idealize, and as a consequence, anyone hoping to understand the ways in which they approximate truth must first subject these conventions to serious consideration. In this and perhaps other ways, those interested in the nature of scientific knowledge may find illumination in positive analogies to the nature of representation in art.

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⁹For a more leisurely route to this conclusion, see Chakravartty (2007, Part III).

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